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Optimization of process variables in electric discharge machining (EDM) using Taguchi methodology

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The present study engrossed with the functional relationship between the input and output parameters of the electric discharge machining (EDM). Four controllable machining parameters, viz. gap voltage (A), current (I_p), duty cycle (C) and pulse on time (T_{on}) have been chosen to ascertain the electrode wear rate (EWR) and surface roughness (SR) of AISI 420 material with copper electrode. Through Taguchi method, a design of experiment developed and it has been used to perform the experiment based on L16 orthogonal array (OA). During machining of AISI420, the highest influencing factor in EWR is I_P and least is C. Similarly, for SR T_{on} is most and C is least significant factor. From analysis of variance (ANOVA), for EWR, I_P is having most significant 79.43% contribution and C is having least significant 2.36 % contribution. Similarly, for SR, T_{on} is having most significant 39.95% contribution and A is having least significant 11.79 % contribution.

Keywords: EDM, AISI420 steel, Taguchi Method, ANOVA

1 Introduction

Non - traditional methods (NTM) have been widely used due to growing need of precision machining of high strength materials¹. NTM offers superior machining capabilities in comparison to conventional machining processes and offers economical and practical viable suitability for solutions in case of complex and intricate shapes². Since the inception, newer methods are being developed by researchers to offer machining solution to newer developed materials. These processes take part a distinguished character in the tool making, die making, aircraft and automobile industries. Now, It is recognized as a normal machining process for manufacturing different tools to produce dies, machining of tool steels (heat treated), metal matrix composites (MMC), super alloys and ceramics requiring high exactness, complicated shapes with high surface finish etc., because of its excellent machining characteristics and high correctness which can't be done by other conventional machines³. Though working principle of EDM (Fig. 1) has already been discussed in past by researchers, authors attempt hereby to briefly outline the working principle of EDM for better understanding of readers⁴. EDM includes material removal employing controlled

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discharge through a gap (approx. $10 - 50 \mu m$) with fluid between workspiece and an electrode. Discussion about EDM principle and working has been made by the researchers earlier⁵.

Table 1 presents briefly important research produced by several researchers⁶⁻²³ in the preceding few years along with remarkable result (s) to give way for the research work shown in this article. This helps the authors in identifying the different process variables and output parameters in order to optimize the process under question.

Authors have worked for extensive literature review of the problem concerned and found that very limited work has been performed by the researchers



Fig. 1 — Schematic diagram of EDM.

a1				d research work	
SI. No.	Author (s)	Work piece	Electrode	Performance	Salient Outcome (s)
	(Year)	material	material	parameters	
1	Mohd Amri Lajis <i>et al.</i>	Tungsten Carbide	Graphite	MRR	Studied the effect of I_p and T_p on EWR, SR and
	$(2009)^6$			EWR	MRR.
				SR	
2	Sanjeev Kumar &	OHNS type die	Cu	SR	Described the effect of I _p , T _{on} , T _{off} and P' of the
	Rupinder Singh $(2010)^7$	steel			tool electrode on SR.
3	S Prabhu & B.K.	Inconel-825	Cylindrical	SR	Better surface finish and reduced micro cracks
	Vinayagam (2011) ⁸	(Nickel alloy)	copper rod		obtained.
4	Razak M.A. <i>et al.</i>	•	Cu	SR	$T_{on} \& T_{off}$ most and least significant factor to
т	$(2016)^9$	alloy	Cu	SIC	affect SR respectively.
5	S Marichamy <i>et al.</i>		Cu	MDD	
5		$\alpha - \beta$ Brass	Cu	MRR	I _p most significant factor to affect MRR,
	$(2016)^{10}$	(Duplex Brass)		EWR	EWR & SR.
				SR	
6	Jeykrishnan. J et al.	EN24 tool steel	Nickel platted	MRR	I _d affect both MRR and SR significantly.
	$(2016)^{11}$		copper	TWR	
7	Banh Tien Long et al.	SKT4, SKD61,	Cu	MRR	Maximize MRR.
	$(2016)^{12}$	SKD11 die steels	Gr		
			Ti Powder		
8	Kumar P. and Parkash R	$Al-B_4C$ composite	Cu	MRR	Investigated effect of I _p , T _{on} and Electrode
	$(2016)^{13}$	· •	EN-19	SR	material on MRR, EWR and SR.
			Graphite	EWR	,
9	B Koteswararao et al.	High carbon Alloy		MRR	I _d most influencing factor on MRR, EWR and
-	$(2017)^{14}$	Steel (EN31)	cu	EWR	Overcut (OC).
	(2017)			OC	() () () () () () () () () ()
10	Chandramouli S (2017) ¹⁵	17-4 PH Steel	Cu-W	MRR	Analyzed control of parameters on MRR & SR
10		1/-411150001	Cu-w	SR	A maryzed control of parameters on where a site
11	Pallavi Chaudhury et al.	EN 10	Cu-W	MRR	Used Taguchi method to optimize the paramete
11	$(2017)^{16}$	LIN-19	Cu-w	TWR	of EDM.
	(2017)			OC	OI EDM.
10		N 04 4 1	D		
12	Abhijit Saha and Subhas	Nano Structured	Brass	MRR	Studied effect of different wires on MRR, MT
	Chandra Mondal (2017) ¹⁷	-	(Conventional)		and surface ¹⁷ .
		Material	and Zinc-coated	IMT	
		(NanoCarb 110)	wire		
13	Ugrasen G <i>et al.</i> (2018) ¹⁸	SS304 (thickness	Molybdenum	MRR	Optimized the process parameters.
		30 mm, 40mm)	wire	SR	
				Accuracy	
14	K Singh et al. (2018) ¹⁹	AISI H-13	zinc coated	MRR	Examined the effect of T _{on} , I _p on SR & MRR.
	,		diffused and	SR	, F
			Soft brass wire		
15	Sagar Patel et al. (2018) ²⁰	Inconel 718	Cu-W	MRR	Optimized MRR, TWR and SR using Taguchi
10	Sugui 1 ator et al. (2010)		eu w	TWR	methodology.
				SR	memodology.
16	Chandramouli S.,	17-4 PH steel	Cu-W	MRR	Studied the effect of T_{op} , T_{off} & I_d on MRR and
10	Eswaraiah K. $(2018)^{21}$	1/-4111 SICCI	(20:80 grade)	SR	Studied the effect of Γ_{on} , $\Gamma_{off} \propto I_d$ on MKK and SR.
17		T: (A1 AV			
17	Praveena T, Prasanna J	Ti-6Al-4V	Cu	MRR	Optimized the MRR, TWR and OC using
	$(2019)^{22}$			TWR	Taguchi Method.
			_	OC	
18	Ezeddini S et al.	Recycled Titanium	Brass wire	MRR	MRR and KW largely affected by Speed of
	$(2019)^{23}$	based composite		Kerf width	advance and servo voltage.
		(an alloy Ti17)			

using the AISI 420 grade steel for different issues for machining like SR, material removal rate (MRR) and EWR *etc.* The material, AISI 420 is found to have comparable mechanical properties to other grades of steel like AISI 304 and AISI 316, but offers higher hardness and thermal conductivity making it suitable for different applications like making dies, cutting tools, surgical instruments, pump shafts and steel balls *etc.*

In this paper, a EDM process is explained with four controllable process parameters, while machining of the AISI 420 with copper electrode as it has been brought up above that several researchers have been investigation worked out on the EDM process on different materials, but not above mentioned material machined with cu electrode. Hence the objective of the presented study to discuss different machining conditions for AISI 420 using EDM and presenting optimal combination of process variables (viz. A, I_P, C and T_{on}) over the output variables (viz. EWR and SR, respectively) using Taguchi methodology.

2 Experimental methodology

The workpiece used for the experiments is made of AISI 420 and is being used at temperature exceeding 427 °C due to rapid softening and loss of corrosion resistance. Nominal details of the experimental setup, workpiece and methodology adopted have been presented in Fig. 2. The properties of tool electrode material, Chemical composition and physical properties of AISI 420 are specified in Tables 2 and 3, respectively.

Experiments have been conducted by using Taguchi L16 OA where total four parameters



399

(J/kg.K)

386

8.9

Copper

considered as four-level were selected to analyse the influence of the parameters on the responses. Input process parameters and their levels are shown in Table 4. Every experiment has been performed three times for each experimental run to minimize any kind of error incurred and their average value is taken into account

2.1 Relevance of output variables

- The EWR is indicator of the volume of electrode removed per unit time during the machining operation and its increase with respect to time results in increased productivity.
- b. SR is a indication of the irregularities in the surface and is a surface texture. It is computed in terms of vertical deviations of the real surface from its ideal surface.
- c. The four controllable parameters were optimized using MINITAB 19.0 software.

3 Taguchi L16

With growing industrial need and consistent thrust over optimal utilization of machining facilities available, different optimization techniques have been employed of which, Taguchi method is prominently used²⁴. It has been considered as one of simple technique with reliable, systematic and efficient tool for optimization of different process parameters including machining processes²⁵. A schematics of above mentioned steps has been discussed briefly in Fig. 3.

Table 4 — Machining parameters and their levels for experimentation.							
Input Unit Code Range				Levels and Values			
Parameters			(as specified by Machine Manufacturer)	1	2	3	4
Gap voltage	Volt (V)	А	15-150	15	45	75	105
Current	Ampere (A)	I_P	0-10	2	4	6	8
Duty Cycle	%	С	8-96	24	48	72	96
Pulse on time	µsec	T _{on}	0.5-2000	50	100	150	200

	Table 3 — Chemical composition and physical properties of AISI420.							
	Chemical composition of AISI420							
Carbon	Silicon	Manganese	Chromium	Phosphorous	Sulphur			
0.23	0.384	0.310	13.208	0.040	0.030			
		Physical Proper	ties of AISI420					
Density (gm/cc)	Specific heat (KJ/kg.K)	Thermal conductivity (W/mK)	Hardness (HRC)	Tensile strength (MPa)	Elongation %			
7750	0.46	24.9	33	1120	18.2			

(u-ohms)

1.69

48



Fig. 3 — Basic steps for Taguchi methodology.

The technique involves application of OA experiments with reduced variance for the experiment designed with optimal setting. Hence, it is aimed to obtain best optimal results with design of experiments using Taguchi method. OA provides optimal number of experiments and calculation of S/N ratio (SNR), which is a log function of desired output of the objective function²⁶.

For larger the better (LTB) (maximize response), the model equation is as follows:

$$\eta = -10 \log_{10} \left(\frac{1}{n} \sum_{i=1}^{n} \frac{1}{y_i^2} \right) \qquad \dots (1)$$

For smaller the better (STB) (minimize response), the model equation is as follows:

$$\eta = -10 \log_{10} \left(\frac{1}{n} \sum_{i=1}^{n} y_i^2 \right) \qquad \dots (2)$$

Taguchi method alters the values of objective function to SNR as a measure of the performance characteristics of the experiment²⁷. ANOVA evaluates parameters [like Degree of freedom (DOF), sum of square (SS)], variance and percentage of individual factor. SS covers deviation between test data and mean value of data. The Fisher's ratio (F value) is calculated using F test, which indicates the quantum of effect of a parameter over the performance characteristics²⁸. The L16 OA for the experiment is shown is Table 5.

	,	Table 5 — L16	OA.	
		Fac	tors	
L	А	Ip	С	Ton
1	1	1	1	1
2	1	2	2	2
3	1	3	3	3
4	1	4	4	4
5	2	1	2	3
6	2	2	1	4
7	2	3	4	1
8	2	4	3	2
9	3	1	3	4
10	3	2	4	3
11	3	3	1	2
12	3	4	2	1
13	4	1	4	2
14	4	2	3	1
15	4	3	2	4
16	4	4	1	3

4 Evaluation of data

In Taguchi method, the higher the levels for SNR, the stabler the overall performance it implies that the factor levels with the most leading SNR value should forever be chosen. Regardless of the STB / LTB, the higher variety characteristics, the greater SNR corresponds to the less variance of the response characteristics around the objective value. The use of SNR is to measure responses to refine products and processes indifferent to the noise factor. This indicates the degree of predictable responses of product or process in the presence of noise factors. The parameters were set with the highest SNR yield optimum value with minimum variance. The experimental results and their SNR values are shown in Table 6. LTB function is used for MRR to enhance productivity and STB is for SR and EWR. The SR characteristics to find the arithmetic mean average surface roughness (Ra). The maximum level for a factor is the level that appears in the largest SNR value in thetest field.

4.1 Analysis of S/N Ratios

In this machining process, the lowest EWR having 75 volt, 2 ampere, 72 %, 200 μ sec as input variables and similarly, the lowest SR having corresponding input variables *viz.* 15 volt, 2 ampere, 24% and 50 μ sec. From Table 7 shows that for EWR, IP is the most and C is the least significant factor. Similarly, Table 8 shows that for SR, Ton is most, and C is the least significant

			Table 6 –	- The experim	ents results and SNR	values.		
Run	А	I_P	С	Ton	EWR (gm/min)	SNR (dB)	SR (µm)	SNR (dB)
1	15	2	24	50	0.0003	69.420942	14.18	-23.0335
2	15	4	48	100	0.0018	55.139239	33.36	-30.4645
3	15	6	72	150	0.0025	52.0412	29.46	-29.3847
4	15	8	96	200	0.0025	52.0412	34.98	-30.8764
5	45	2	48	150	0.0003	70.370279	32.37	-30.2029
6	45	4	24	200	0.0012	58.757042	35.77	-31.0704
7	45	6	96	50	0.0052	45.679933	26.25	-28.3826
8	45	8	72	100	0.0033	49.542425	20.04	-26.038
9	75	2	72	200	0.00022	73.06425	33.73	-30.5603
10	75	4	96	150	0.0004	67.234557	36.73	-31.3004
11	75	6	24	100	0.0012	58.329079	27.6	-28.8182
12	75	8	48	50	0.0024	52.395775	27.36	-28.7423
13	105	2	96	100	0.0006	64.349679	17.55	-24.8855
14	105	4	72	50	0.0006	63.806634	24.08	-27.6331
15	105	6	48	200	0.0025	52.0412	22.91	-27.2005
16	105	8	24	150	0.0020	53.9794	33.11	-30.3992
	Table 7 –	- S/N response	table for EWR	•			Plots for SN ratios Ita Means	
Level	А	I_P	С	T _{on}	A	lp	С	Ton
1	57.16	69.30	60.12	57.83	70 -	1		
2	56.09	61.23	57.49	56.84	05			
3	62.76	52.02	59.61	60.91	<u>85</u>			
4	58.54	51.99	57.33	58.98	× 60	\setminus \downarrow		×
Delta	6.67	17.31	2.80	4.07	Mean of SN ratios	- > + -		+
Rank	2	1	4	3	₩ ₅₅			
	Table 8	— S/N respons	e table for SR.		-		-•	
Level	А	I _P	С	Ton	50-L 15 45 75	5 105 2 4 6	8 24 48 72 9	8 50 100 150
1	-28.44	-27.17	-28.33	-26.95	Signal-to-noise	: Smaller is better		

factor. The observed value of EWR is 0.00022 gm/min, and the calculated value of SNR from Taguchi analysis is found to be -73.06425 dB. Similarly, for SR, the observed value is 14.18µm, and the calculated value of SNR from Taguchi analysis is found to be -23.034 dB. Hence the like input factors are most optimized controllable parameters.

-30.12

-28.45

-29.01

2.95

2

-29.15

-28.40

-28.86

0.82

4

-27.55

-30.32

-29.93

3.37

1

2

3

4

Delta

Rank

-28.92

-29.86

-27.53

2.33

3

The factorial effect plots are drawn by considering the mean average of the parameters of their each level of raw data. Figures (4 & 5) show factorial effect plot for SNR of EWR and SR. Fig. 4 shows that EWR is minimize when A is 75V, I_P is 2 Ampere, C is 24 % and T_{on} is 150 µsec. Similarly, Fig. 5 shows that SR is minimize when A is 105V, I_P is 2 Ampere, C is 24 % and T_{on} is 50 µsec.



4.2 ANOVA

The main objective of ANOVA is to classify the impact of individual and interaction factors. Table shows the analysis ANOVA for EWR and SR. This investigation is taken out for 95 % confidence level *i.e.*, 5 % significance level. Based on the F-Statistics,

Table 9 — ANOVA for EWR.							
Source	DF	Seq SS	Contribution	Adj SS	Adj MS	F- Value	P- Value
А	3	1.3602	9.78%	1.3602	0.4534	1.98	0.295
I_P	3	11.0495	79.43%	11.0495	3.6832	16.08	0.024
С	3	0.3287	2.36%	0.3287	0.1096	0.48	0.720
Ton	3	0.4852	3.49%	0.4852	0.1617	0.71	0.609
Error	3	0.6871	4.94%	0.6871	0.2290		
Total	15	13.9107	100.00%				
		Table 1	0 — Model s	ummary f	for EWF	R.	
	S		R-sq		R·	-sq(adj)	1
0.4	4785	583	95.06%)	7	5.30%	
		Та	ble 11 — AN	OVA for	SR.		
Source	DF	Seq SS	Contribution	Adj SS	Adj MS	F- Value	P- Value
А	3	523.46	11.79%	523.46	174.49	16.41	0.023
I_P	3	1561.85	35.16%	1561.85	520.62	48.96	0.005
С	3	549.78	12.38%	549.78	183.26	17.24	0.021
Ton	3	1774.59	39.95%	1774.59	591.53	55.63	0.004
Error	3	31.90	0.72%	31.90	10.63		
Total	15	4441.57	100.00%				
		Table	12 — Model s	summary	for SR.		
S			R-sq		R-sq(adj)		
3.26074			99.28%	96.41%			
Table 13 — Optimal parameter setting of process parameters.							
Output parameters			Optin	nal comb	oination		
]	Level	A I	Р	С	Ton
Min. EV	NR	A3I _I	o1C1T _{on} 3	75 2	2 2	24	150
Min. SF	ł	A4 I _P	1C1 T _{on} 1 1	05 2	2 2	24	50

define the process parameter is important or not at a selective confidence level. Larger F-Statistics showed that the modification of process parameters made a significant change on the performance. R Square describes the range to which input parameters intercept the modification of the output response and predicted variable. For a good model, R sq. should be high value. From Tables 9 and 10, it can be concluded that for EWR, I_P had the most significant 79.43 % contribution and C the least significant 2.36 % contribution. Similarly, from Tables 11 and 12, it can be concluded that for SR, Ton had the most significant 39.95 % contribution and A the least significant 11.79 % contribution and the remaining parameters were found insignificant. Table 13 displays, the optimal setting of process parameters.

Tabl	Table 14 — Results of validation test.					
	EWR(gm/min) SR(µm)					
Level	A3I _P 1C1T _{on} 3	A4IP1C1 Ton1				
Predicted	0.00021	14.02				
Experimental	0.00022	14.18				
Error (%)	4.54	1.12				

4.3 Validation test

The optimum level of the process parameters is obtained in the previous section. Next move is to confirm the percentage variation of EWR and SR between the primary setting and for this optimal sequence. Table 14 parallels the results of the validation trials using the optimal process parameters. For EWR and SR, there some error exists in Table 14. The total mean of EWR decreased from 0.00022 gm/min to 0.00021 gm/min for optimal machining parameters of A3IP1C1Ton3 and also fell of SR from 14.18 μ m to 15.08 μ m for machining parameters of A4IP1C1Ton1 which confirms that right combination of the process parameters to the minimization of EWR and SR of the machined surface.

The predicted and experimental values for EWR and SR are shown in Table 14. It validates that the error between the confirmatory and predicted value is less than 5 %. It verifies that remarkable reproducibility of the results and also confirms that the optimized process parameters and response values are in close alliance with experimentally obtained values.

5 Conclusions

The experimental investigation of EDM on AISI 420 has been done using Taguchi technique. Four important process parameters A, I_P , C and T_{on} have been studied. The following conclusions are made:

- (i) During machining of AISI420, the highest influencing factor in EWR is I_P and least is C. Similarly, for SR T_{on} is most and C is least significant factor.
- (ii) The optimal levels of the four factors have been established to get optimal EWR and SR using L16 OA.
- (iii) For EWR, The result showed that the A of 105 volt, I_P of 1ampere, C of 16% and T_{on} 200 µsec bears the optimal quality characteristics. Similarly, for SR, The result showed that the A of 135 volt, I_P of 1ampere, C of 16% and T_{on} 5 µsec bears the optimal quality characteristics.
- (iv) From ANOVA, for EWR, I_P is having most significant 79.43 % contribution and C is having least significant 2.36 % contribution. Similarly,

for SR, T_{on} is having most significant 39.9 5% contribution and A is having least significant 11.79 % contribution.

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